

Artificial Intelligence and Economic Growth

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What are the implications of A.I. for economic growth?

- Build some growth models with A.I.
 - A.I. helps to make goods
 - A.I. helps to make ideas
- Implications
 - Long-run growth
 - Share of GDP paid to labor vs capital
 - Firms and organizations
- Singularity?

Two Main Themes

- A.I. modeled as a continuation of automation
 - Automation = replace labor in particular tasks with machines and algorithms
 - *Past*: textile looms, steam engines, electric power, computers
 - *Future*: driverless cars, paralegals, pathologists, maybe researchers, maybe everyone?
- A.I. may be limited by Baumol's cost disease
 - *Baumol*: growth constrained not by what we do well but rather by what is essential and yet hard to improve

Simple Model of Automation (Zeira 1998)

- Production uses n tasks:

$$Y = AX_1^{\alpha_1} X_2^{\alpha_2} \cdot \dots \cdot X_n^{\alpha_n},$$

where $\sum_{i=1}^n \alpha_i = 1$ and

$$X_{it} = \begin{cases} L_{it} & \text{if not automated} \\ K_{it} & \text{if automated} \end{cases}$$

- Substituting gives

$$Y_t = A_t K_t^\alpha L_t^{1-\alpha}$$

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- Comments:
 - α reflects the *fraction of tasks that are automated*
 - Embed in neoclassical growth model \Rightarrow

$$g_y = \frac{g_A}{1 - \alpha} \quad \text{where} \quad y_t \equiv Y_t/L_t$$

- Automation: $\uparrow \alpha$ raises both capital share and LR growth
 - Hard to reconcile with 20th century
 - Substantial automation but stable growth and capital shares

Subsequent Work

- Acemoglu and Restrepo (2017)
 - Old tasks are gradually automated as new (labor) tasks are created
 - Fraction automated can then be steady
 - Rich framework, with endogenous innovation and automation
- Peretto and Seater (2013), Hemous and Olson (2016), Agrawal, McHale, and Oettl (2017)

Baumol's Cost Disease and the Kaldor Facts

- Baumol: Agriculture and manufacturing have rapid growth and declining shares of GDP
 - ... but also rising automation
- Aggregate capital share could reflect a **balance**
 - Rises within agriculture and manufacturing
 - But falls as these sectors decline
- Maybe this is a general feature of the economy!
 - First agriculture, then manufacturing, then services

Model

- Production is CES in tasks, with $EofS < 1$ (complements)

$$Y_t = A_t \left(\int_0^1 X_{it}^\rho di \right)^{1/\rho} \quad \text{where } \rho < 0 \quad (\text{Baumol})$$

- Let β_t = fraction of tasks automated by date t :

$$Y_t = A_t \left[\beta_t \left(\frac{K_t}{\beta_t} \right)^\rho + (1 - \beta_t) \left(\frac{L}{1 - \beta_t} \right)^\rho \right]^{1/\rho}$$

$$\implies Y_t = A_t ((B_t K_t)^\rho + (C_t L)^\rho)^{1/\rho}$$

where $B_t = \beta_t^{\frac{1}{\rho}-1}$ and $C_t = (1 - \beta_t)^{\frac{1}{\rho}-1}$

- **Note:** increased automation $\Rightarrow \downarrow B_t$ and $\uparrow C_t$ since $\rho < 0$.
(e.g. a given amount of capital is spread over more tasks.)

Factor Shares of Income

- Ratio of capital share to labor share:

$$\frac{\alpha_{K_t}}{\alpha_{L_t}} = \left(\frac{\beta_t}{1 - \beta_t} \right)^{1-\rho} \left(\frac{K_t}{L_t} \right)^\rho$$

- Two offsetting effects ($\rho < 0$):
 - $\uparrow \beta_t$ raises the capital share
 - $\uparrow K_t/L_t$ lowers the capital share

If these balance, constant factor shares are possible

Automation and Asymptotic Balanced Growth

- Suppose a constant fraction of non-automated tasks become automated each period:

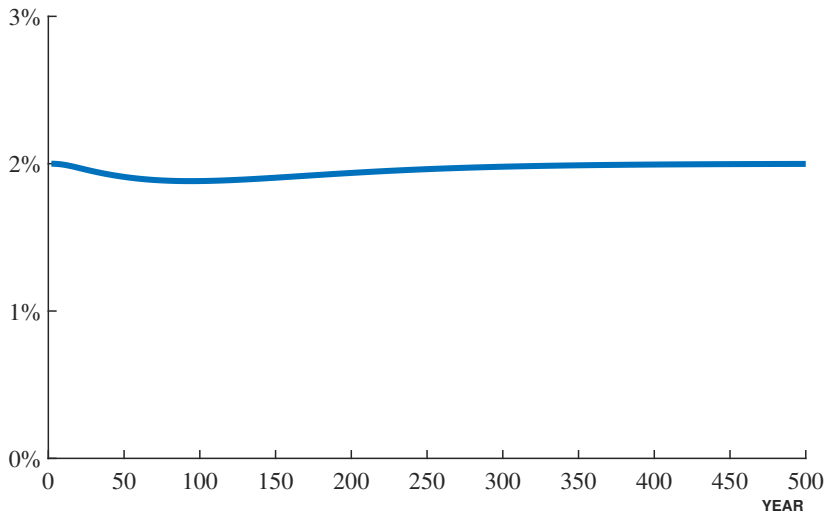
$$\dot{\beta}_t = \theta(1 - \beta_t)$$

Then $\beta_t \rightarrow 1$ and C_t grows at a constant rate!

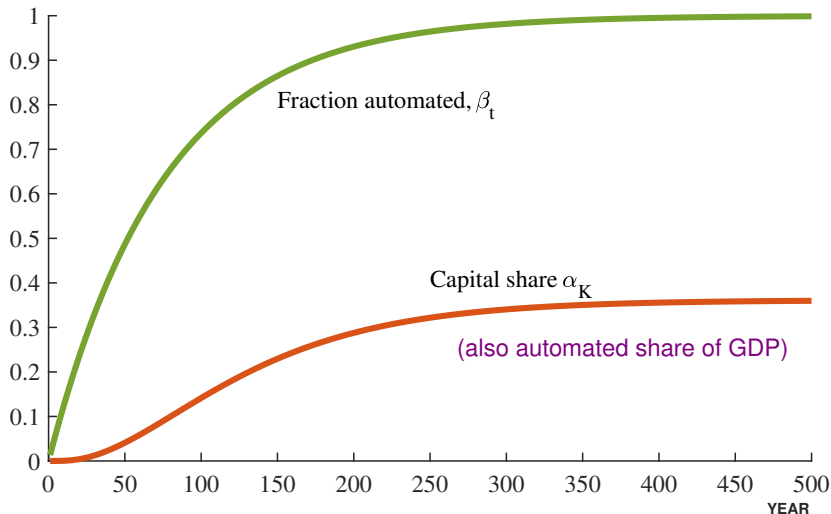
- With $Y_t = F(B_t K_t, C_t L_t)$, balanced growth as $t \rightarrow \infty$:
 - All tasks eventually become automated
 - Labor still gets 2/3 of GDP! Vanishing share of tasks, but all else is cheap (Baumol)
 - Agr/Mfg shrink as a share of the economy...

Simulation: Automation and Asymptotic Balanced Growth

GROWTH RATE OF GDP



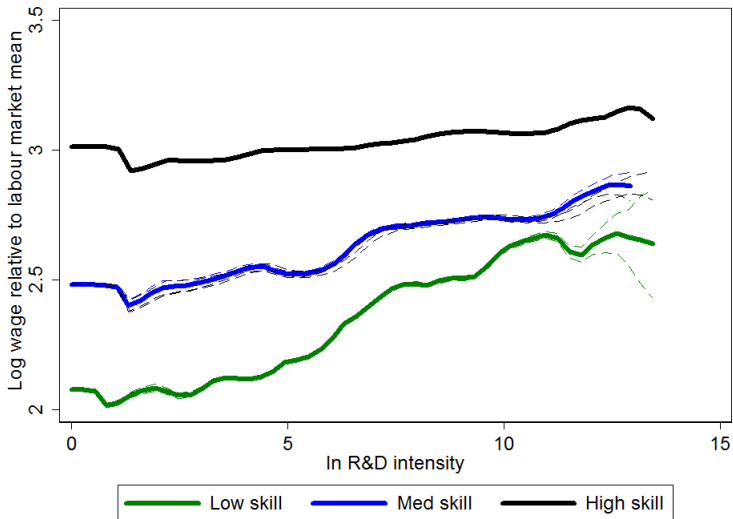
Simulation: Capital Share and Automation Fraction



AI, Organizations, and Wage Inequality

- Usual story: robots replace low-skill labor, hence \uparrow skill premium (e.g., Krusell et al. 2000)
- But solving future problems, incl. advancing AI, might be increasingly hard, suggesting \uparrow complementarities across workers, \uparrow teamwork, and changing firm boundaries (Garicano 2000, Jones 2009)
- Aghion et al. (2017) find evidence along these lines
 - outsource higher fraction of low-skill workers
 - pay *increased* premium to low-skill workers kept

AI, Organizations, and Wage Inequality



AI in the Ideas Production Function

- Let production of goods and services be $Y_t = A_t L_t$
- Let idea production be:

$$\dot{A}_t = A_t^\phi \left(\int_0^1 X_{it}^\rho di \right)^{1/\rho}, \quad \rho < 0$$

- Assume fraction β_t of tasks are automated by date t . Then:

$$\dot{A}_t = A_t^\phi F(B_t K_t, C_t S_t)$$

where

$$B_t \equiv \beta_t^{\frac{1-\rho}{\rho}}; C_t \equiv (1 - \beta_t)^{\frac{1-\rho}{\rho}}$$

- This is like before...

AI in the Ideas Production Function

- Intuition: with $\rho < 0$ the scarce factor comes to dominate

$$F(B_t K_t, C_t S_t) = C_t S_t F\left(\frac{B_t K_t}{C_t S_t}, 1\right) \rightarrow C_t S_t$$

- So, with continuous automation

$$\dot{A}_t \rightarrow A_t^\phi C_t S_t$$

- And asymptotic balanced growth path becomes

$$g_A = \frac{g_C + g_S}{1 - \phi}$$

- We get a “boost” from continued automation (g_C)

Singularities

- Now we become more radical and consider what happens when we go “all the way” and allow AI to take over all tasks.
- **Example 1:** Complete automation of goods and services production.

$$Y_t = A_t K_t$$

→ Then growth rate can accelerate exponentially

$$g_Y = g_A + sA_t - \delta$$

we call this a “Type I” growth explosion

Singularities

- **Example 2:** Complete automation in ideas production function

$$\dot{A}_t = K_t A_t^\phi$$

- Intuitively, this idea production function acts like

$$\dot{A}_t = A_t^{1+\phi}$$

- Solution:

$$A_t = \left(\frac{1}{A_0^{-\phi} - \phi t} \right)^{1/\phi}$$

- Thus we can have a true **singularity** for $\phi > 0$. A_t exceeds any finite value before date $t^* = \frac{1}{\phi A_0^\phi}$.

Objections to singularities

- 1 Automation limits (no $\beta_t \rightarrow 1$)
- 2 Search limits

$$\dot{A}_t = A_t^{1+\phi}$$

but $\phi < 0$ (e.g., fishing out, burden of knowledge...)

- 3 Natural Laws

$$Y_t = \left(\int_0^1 (a_{it} Y_{it})^\rho \right)^{1/\rho} \quad \text{where } \rho < 0$$

now can have $a_{it} \rightarrow \infty$ for many tasks but no singularity (cf. Moore's Law vs. Carnot's Theorem)

- *Baumol theme*: growth determined not by what we are good at, but by what is essential yet hard to improve

Conclusion: A.I. in the Production of Goods and Services

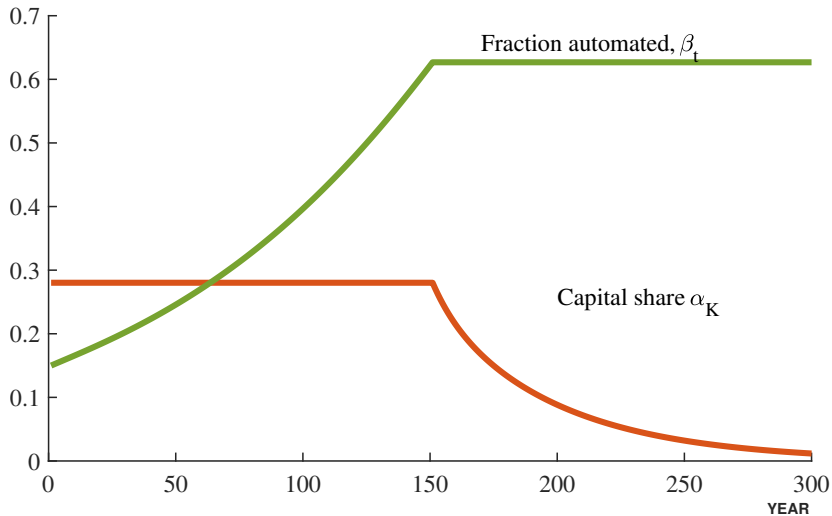
- Introduced Baumol's "cost disease" insight into Zeira's model of automation
 - Automation can act like labor augmenting technology (surprise!)
 - Can get balanced growth with a constant capital share well below 100%, even with nearly full automation
- Considered effects on wage inequality and firm organization. More AI-intensive firms could:
 - Outsource a higher fraction of low-occupation tasks
 - Pay \uparrow premium to low-occupation workers they keep

Conclusion: A.I. in the Ideas Production Function

- Could A.I. obviate the role of population growth in generating exponential growth?
- Discussed possibility that A.I. could generate a singularity
 - Derived conditions under which the economy can achieve infinite income in finite time
- Discussed obstacles to such events
 - Automation limits, search limits, and/or natural laws (among others)

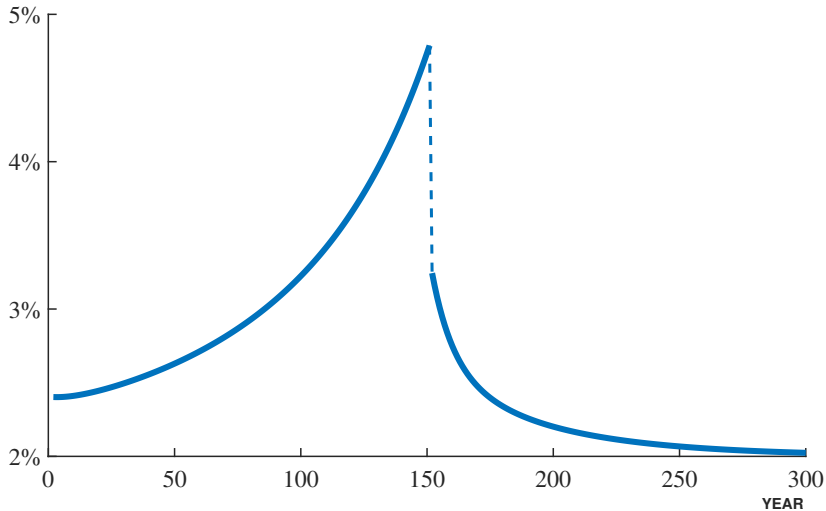
Extra Slides

Constant Capital Share



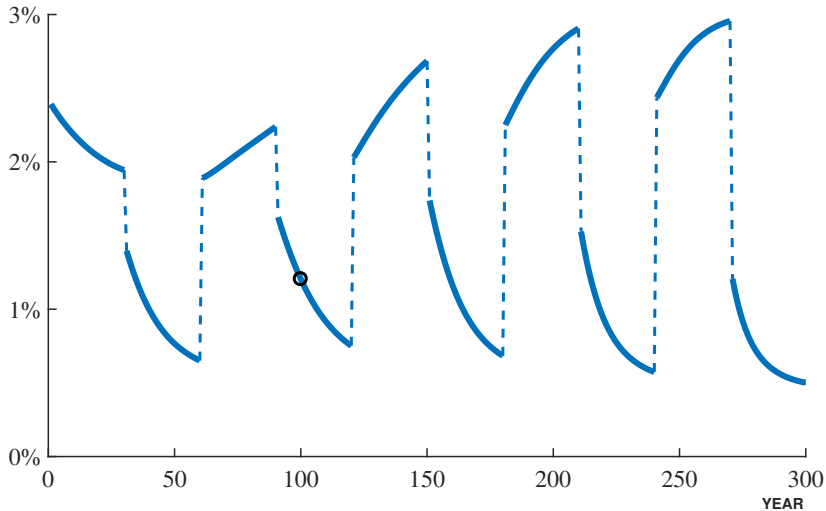
Constant Capital Share

GROWTH RATE OF GDP

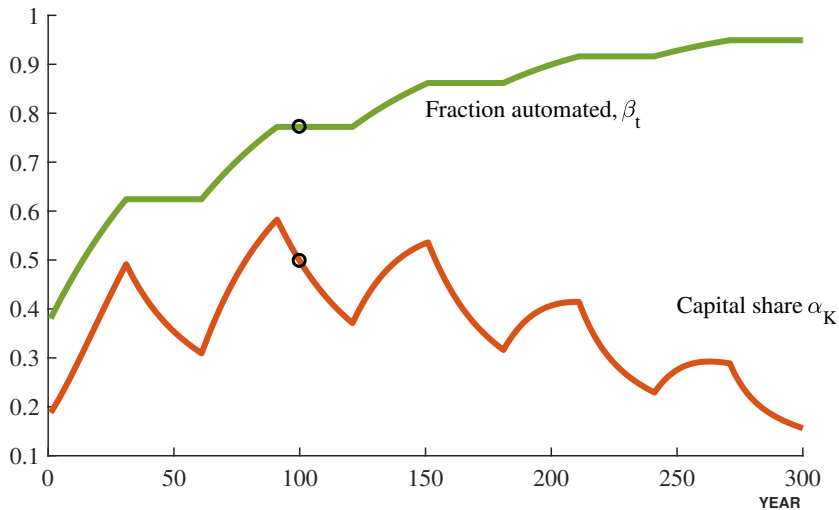


Switching regimes...

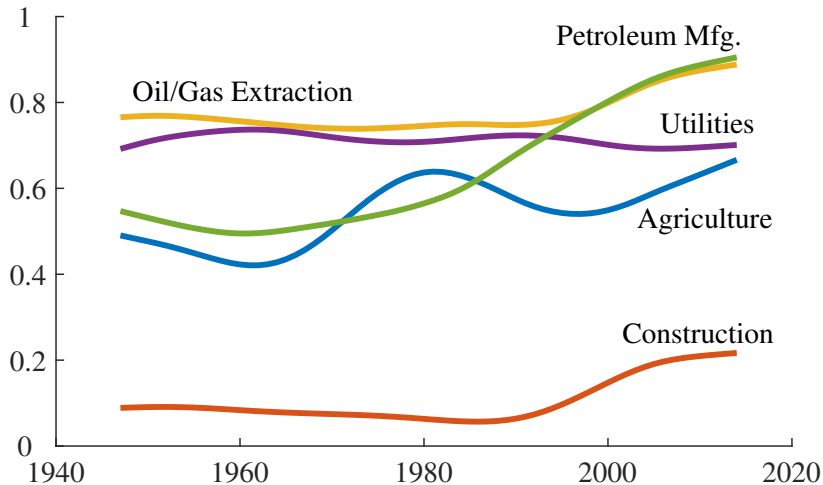
GROWTH RATE OF GDP



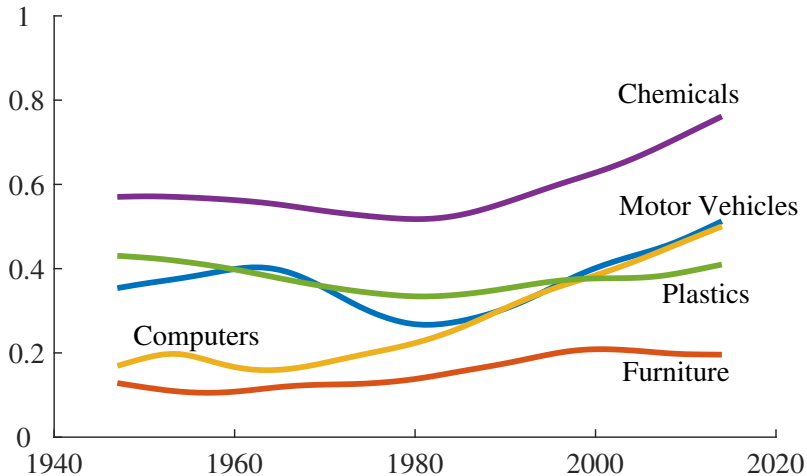
Switching regimes...



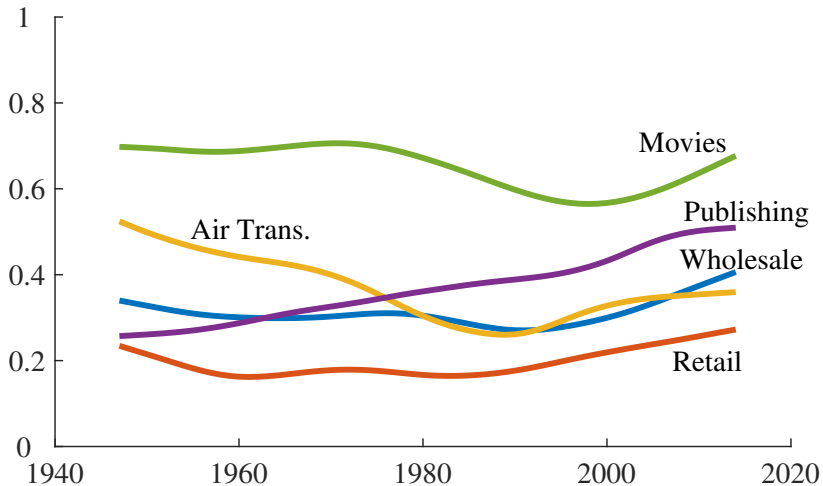
Capital Shares in U.S. Industries



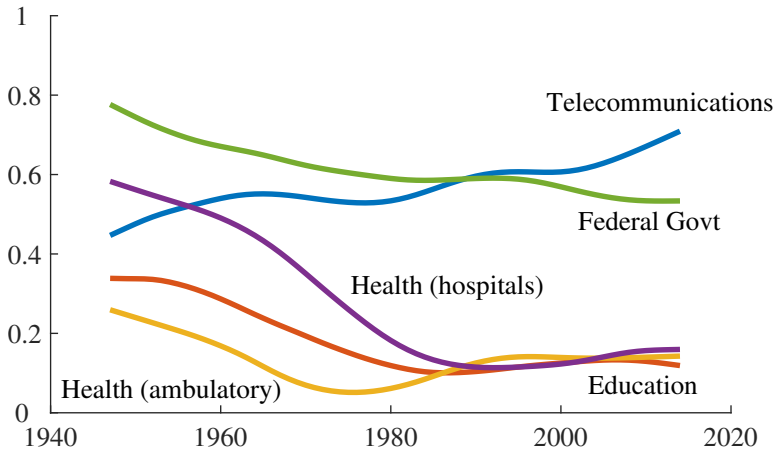
Capital Shares in U.S. Industries



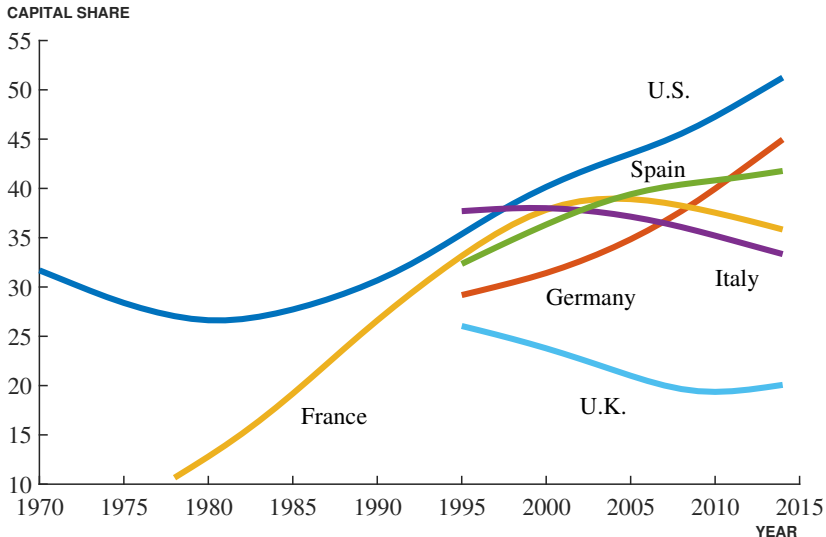
Capital Shares in U.S. Industries



Capital Shares in U.S. Industries



Capital Share of Income: Transportation Equipment



Adoption of Robots and Change in Capital Share

CHANGE IN CAPITAL SHARE

